

Proposed problem

Evaluate

$$\sum_{n=1}^{\infty} \left[n^2 \sum_{k=n+1}^{\infty} \frac{1}{k^2} - n + \frac{1}{2} - \frac{1}{6n} \right]^2$$